Can a square be subdivided into smaller squares no two of which have the same side length? Four Trinity College, Cambridge University undergraduate students worked on this problem in the years 1936-1938. This talk briefly describes the students and their later use of the pseudonym Blanche Descartes. The rest of the talk is about their empirical and theoretical approaches to solving the problem.